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Kuiper Belt Occultation Predictions

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ABSTRACT. Here we present observations of seven large Kuiper Belt objects. From these observations, we extract a point source catalog with $\sim 0.01''$ precision, and astrometry of our target Kuiper Belt objects with $0.04\text{--}0.08''$ precision within that catalog. We have developed a new technique to predict the future occurrence of stellar occultations by Kuiper Belt objects. The technique makes use of a maximum likelihood approach which determines the best-fit adjustment to cataloged orbital elements of an object. Using simulations of a theoretical object, we discuss the merits and weaknesses of this technique compared to the commonly adopted ephemeris offset approach. We demonstrate that both methods suffer from separate weaknesses, and thus together provide a fair assessment of the true uncertainty in a particular prediction. We present occultation predictions made by both methods for the seven tracked objects, with dates as late as 2015. Finally, we discuss observations of three separate close passages of Quaoar to field stars, which reveal the accuracy of the element adjustment approach, and which also demonstrate the necessity of considering the uncertainty in stellar position when assessing potential occultations.

Online material: color figures

1. INTRODUCTION

Detection of a point-source occultation by a planetesimal can provide a wealth of detail about that body. For example, observations of stellar occultations by Kuiper Belt objects (KBOs) have been used to measure sizes (Elliot et al. 2010; Sicardy et al.

2011), shapes (Braga-Ribas et al. 2011, in press), and atmospheric extents (Hubbard et al. 1988; Elliot et al. 1989) of the occulting KBOs. As the angular extents of most KBOs are approximately $\lesssim 0.03''$, even the largest few are only partially resolved in the highest resolution telescope imaging possible (Brown & Trujillo 2004). As a result, the information gleaned from an occultation about the occulting body is currently impossible to get by any other means.

The small angular extents of KBOs make it extremely challenging to predict when they will cause an occultation. The best stellar catalogs currently available typically have astrometric accuracies up to an order of magnitude larger than the apparent diameters of the largest KBOs, e.g., $\sim 0.25''$ for USNO B1 (Monet 1998) and $\sim 0.07''$ for the 2MASS catalog (Skrutskie et al. 2006). For reference, $0.1''$ uncertainty in stellar position projected to typical KBO distances of 40 AU results in approximately 3000 km uncertainty in the predicted shadow path. Thus, the use of standard astrometric catalogs can result in path uncertainty larger than the Earth. As done by Stone et al. (1999), the generation of a custom point source catalog is the first step required in producing occultation predictions with any certainty.

An additional source of uncertainty, and equally important as stellar position, is the ephemeris of the KBO in question. As discussed by Stone et al. (1999) for the object (5145) Pholus, ephemeris uncertainty can be as large as $0.5''$ and can nullify any efforts made in producing accurate point-source catalogs. Assafin et al. (2012) present a method by which the nominal

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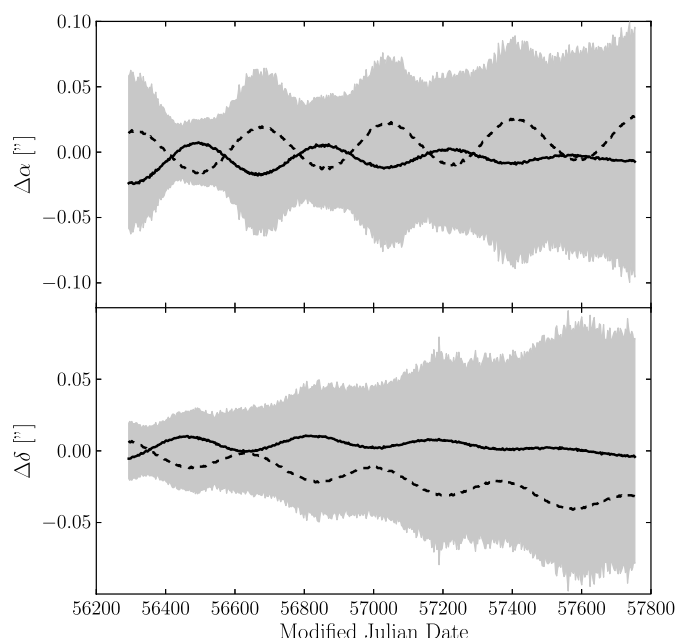


FIG. 1.—Difference in R.A. (*top*) and decl. (*bottom*) as a function of MJD between the actual object ephemeris and that found by the constant offset approach (*dashed line*) and the element correction method (*solid line*) for a simulated observation of a KBO on orbit similar to Eris (see § 2.3). The *grey shaded* region is the ephemeris envelope generated from the 1- σ range of orbital elements derived from the element correction likelihood routine. Note that the envelope only includes the range in ephemerides caused by the uncertain orbital elements, and does not include uncertainty in the position of the potentially occulted point source.

ephemeris of an object—evaluated from the *astDys* orbital elements¹⁴—is corrected by a constant vector value which is measured with respect to their point source catalog. This offset is then used to approximately correct the ephemeris to that catalog.

The method presented by Assafin et al. (2012) has been successful in predicting a few detected occultations (see, for example, Braga-Ribas et al. 2011, in press). This method, however, still suffers from uncertainty in the object’s ephemeris. As is shown in Figure 1, the use of a nominal ephemeris can result in oscillations between the predicted and actual position of the body as large or larger than a few tens of milliarcseconds, the apparent diameters of the largest KBOs.

Here we present a method of occultation prediction similar in fashion to that used by Assafin et al. (2012). Rather than adopting a constant ephemeris offset, our method uses high-precision astrometry to correct the nominal orbital elements themselves. Ephemeris uncertainty and orbital element uncertainty are natural end products of our method, unlike other methods which do not produce a formal ephemeris uncertainty. This results in independent and complementary predictions to those of the

constant offset method and a means of assessing the true uncertainty in a given prediction. With this method, we present the results of a pilot study to test the feasibility of our approach. We present a list of candidate stellar occultations for seven KBOs, spanning as late as 2015.

In § 2 we present the general method of occultation prediction. We describe our observations and our method of point-source catalog production. We also describe the method of ephemeris generation, and the net uncertainties resultant from our method. In § 3 we present our occultation predictions and present some observations which confirm the validity of the method. We finish with concluding remarks in § 4.

2. OBSERVATIONS AND PREDICTIONS

In this section we present our observations and predictions method. This program was a pilot study of seven large KBOs: (50000) Quaoar, (84522) 2002 TC302, (90377) Sedna, (136199) Eris, (136472) Makemake, (202421) 2005 UQ513, and (225088) 2007 OR10. These objects are all well-tracked KBOs and have ephemerides determined from reported observations spanning many years. The ephemerides of these objects are typical of the most accurate KBO ephemerides available. As a result, these targets should present a simple test case in which only small corrections to their ephemerides will be necessary for occultation prediction purposes.

The first step in predicting stellar occultations is to generate an astrometrically accurate point-source catalog. For this purpose, observations were taken with MegaPrime on the 3.6 m Canada–France–Hawaii Telescope (CFHT). MegaPrime is a 36 CCD optical imager that provides a fully subsampled ($0.1875'' \text{ pixel}^{-1}$) $1 \times 1^\circ$ field of view. Observations were taken utilizing 45 s exposures in SDSS r' -filter and spanned a region large enough to ensure that the target of interest was within the right ascension (R.A.) and declination (decl.) range throughout 2011 and 2012. Details of the MegaPrime sky coverage can be found in Table 1.

As a result of the CFHT Legacy Survey¹⁵ (Gwyn 2008) the spatial distortions of the MegaPrime field of view are very well understood, and can be well described by a global distortion map with only first and second order terms in radius, as well as individual linear distortion maps for each of the chips in the mosaic. This allows us to determine accurate astrometric distortion maps of the images to be produced. It is from these detrended images that our master point-source catalog (MPSC) is assembled. We describe how this is done in § 2.1.

The MegaPrime images often contain the KBO of interest, and as such also provide some astrometry of the source from which the ephemeris can be corrected. Further tracking observations have been acquired with Gemini Multi-Object Spectrograph (GMOS, Hook et al. 2004) on the 8 m Gemini-North

¹⁴ See <http://hamilton.dm.unipi.it/astdys/>.

¹⁵ See <http://www.cfht.hawaii.edu/Science/CFHTLS/>.

TABLE 1
APPROXIMATE CFHT MEGA PRIME SKY COVERAGE

Object	α_{\min} (deg)	α_{\max} (deg)	δ_{\min} (deg)	δ_{\max} (deg)	Latest predictions ^a	External reference catalog
(50000) Quaoar	261.73	264.27	−15.75	−15.36	2013	2MASS
(84522) 2002 TC302	30.54	22.66	22.26	24.15	2013	2MASS
(90377) Sedna	52.09	54.50	6.48	7.36	2015	SDSS
(136199) Eris	24.40	25.99	−4.35	−2.86	2015	SDSS
(136472) Makemake	189.26	191.82	26.92	27.81	2014	SDSS
(202421) 2005 UQ513	4.24	7.46	28.69	30.76	2013	SDSS
(225088) 2007 OR10	333.92	335.29	−14.38	−13.05	2015	2MASS

NOTE.—Coordinates are in the J2000 reference frame.

^a At least partial coverage of the object's ephemeris during this year.

telescope. Details of the observations presented here are shown in Table 2. These observations are used to correct the nominal orbital elements of each object to produce an extremely

accurate ephemeris in the astrometric system defined by the MPSC. We describe how the element corrections are determined in § 2.3.

TABLE 2
OBJECT ASTROMETRY

MJD	α (deg) ^a	δ (deg) ^a	Coordinate uncertainty (arcsec)
(50000) Quaoar			
55611.655578	262.317292	−15.682684	0.08
55611.657210	262.317310	−15.682681	0.08
55663.553265	262.453589	−15.529130	0.08
55663.554898	262.453576	−15.529122	0.08
55985.641534	263.731585	−15.674959	0.04
55985.642611	263.731593	−15.674956	0.04
55985.643692	263.731603	−15.674958	0.04
55985.644775	263.731610	−15.674948	0.04
56014.560038	263.854030	−15.588429	0.04
56014.561118	263.854034	−15.588423	0.04
56014.589606	263.853980	−15.588339	0.04
56014.590690	263.853977	−15.588332	0.04
56118.285567	262.292690	−15.379824	0.08
56118.286968	262.292638	−15.379842	0.08
56118.464271	262.289430	−15.379901	0.08
56118.465683	262.289404	−15.379892	0.08
(84522) 2002 TC302			
55766.549223	32.684558	22.716384	0.08
55766.552130	32.684566	22.716376	0.08
55768.610035	32.690913	22.729657	0.08
55768.612951	32.690921	22.729677	0.08
55777.535649	32.700664	22.781575	0.08
55802.626603	32.575117	22.874536	0.04
55802.627639	32.575122	22.874536	0.04
55802.628671	32.575101	22.874535	0.04
55808.413270	32.515826	22.884205	0.08
55808.416170	32.515795	22.884211	0.08
55808.587584	32.513837	22.884434	0.08
55808.590500	32.513803	22.884438	0.08
56167.565781	33.379745	23.861149	0.04
56167.566890	33.379726	23.861162	0.04
56167.567966	33.379719	23.861156	0.04

TABLE 2 (Continued)

MJD	α (deg) ^a	δ (deg) ^a	Coordinate uncertainty (arcsec)
56167.569045	33.379709	23.861170	0.04
56167.570125	33.379706	23.861155	0.04
56167.571205	33.379695	23.861175	0.04
56167.572363	33.379676	23.861170	0.04
56167.573443	33.379676	23.861166	0.04
56167.574524	33.379659	23.861179	0.04
(90377) Sedna			
55766.573408	53.498839	6.991800	0.08
55770.605386	53.521642	6.988467	0.08
55772.597075	53.531882	6.986487	0.04
55798.616249	53.600415	6.942037	0.08
55798.617406	53.600414	6.942031	0.08
55802.630832	53.599887	6.932450	0.04
55802.631862	53.599891	6.932445	0.04
55811.575325	53.588023	6.909029	0.08
56166.600171	54.159237	7.070095	0.04
56166.602789	54.159258	7.070093	0.04
56166.603917	54.159248	7.070082	0.04
56166.605121	54.159248	7.070078	0.04
56166.607849	54.159247	7.070067	0.04
56166.610168	54.159244	7.070065	0.04
56166.611296	54.159237	7.070061	0.04
56166.612487	54.159239	7.070061	0.04
56166.613652	54.159246	7.070053	0.04
56166.617210	54.159250	7.070052	0.04
56166.618394	54.159247	7.070043	0.04
56247.334949	53.655513	6.833374	0.04
56247.336107	53.655502	6.833367	0.04
56247.337203	53.655493	6.833367	0.04
56247.338359	53.655486	6.833362	0.04
56247.339439	53.655467	6.833361	0.04
56247.340518	53.655459	6.833361	0.04
56247.341874	53.655446	6.833359	0.04
56247.343063	53.655432	6.833337	0.04
56247.344141	53.655424	6.833354	0.04

TABLE 2 (Continued)

MJD	α (deg) ^a	δ (deg) ^a	Coordinate uncertainty (arcsec)
56247.345223	53.655403	6.833348	0.04
56247.346303	53.655403	6.833338	0.04
56247.347381	53.655386	6.833342	0.04
(136199) Eris			
55766.556284	25.602261	-3.768848	0.08
55768.604971	25.601333	-3.773118	0.08
55777.540434	25.589507	-3.794366	0.08
55798.486896	25.514069	-3.857934	0.08
55798.630434	25.513314	-3.858422	0.08
55802.480507	25.492609	-3.871678	0.04
55802.481538	25.492597	-3.871693	0.04
55802.482653	25.492594	-3.871686	0.04
55808.409195	25.456987	-3.892695	0.08
55808.580605	25.455872	-3.893299	0.08
56161.606367	25.652157	-3.591412	0.04
56161.607444	25.652158	-3.591421	0.04
56163.593624	25.642338	-3.598028	0.04
56163.594707	25.642339	-3.598037	0.04
56163.595783	25.642330	-3.598044	0.04
56163.596861	25.642332	-3.598044	0.04
56163.597941	25.642308	-3.598038	0.04
56163.600103	25.642292	-3.598039	0.04
56163.604420	25.642286	-3.598057	0.04
56163.608742	25.642269	-3.598078	0.04
56163.609826	25.642262	-3.598085	0.04
56163.619655	25.642180	-3.598105	0.04
56163.622955	25.642186	-3.598131	0.04
56165.465516	25.632600	-3.604358	0.04
56165.466591	25.632608	-3.604352	0.04
(136472) Makemake			
55973.644682	190.974085	27.297554	0.04
55985.608243	190.816955	27.419601	0.04
55985.609359	190.816934	27.419614	0.04
55985.612684	190.816894	27.419645	0.04
55985.616096	190.816843	27.419663	0.04
55985.617177	190.816818	27.419690	0.04
55985.624423	190.816726	27.419742	0.04
55985.625504	190.816708	27.419747	0.04
56001.535272	190.566893	27.561053	0.04
56001.536352	190.566867	27.561055	0.04
56001.537443	190.566844	27.561069	0.04
56030.539757	190.064060	27.720943	0.04
56030.540836	190.064051	27.720934	0.04
56030.543005	190.064007	27.720949	0.04
56326.479428	191.949982	26.705260	0.04
56326.480505	191.949975	26.705269	0.04
56326.481599	191.949959	26.705275	0.04
56326.482708	191.949958	26.705285	0.04
56326.483785	191.949948	26.705309	0.04
56326.488112	191.949909	26.705350	0.04
(202421) 2005 UQ513			
55766.542406	6.328121	29.393568	0.15
55766.545329	6.328108	29.393587	0.15
55769.575632	6.307870	29.413344	0.15

TABLE 2 (Continued)

MJD	α (deg) ^a	δ (deg) ^a	Coordinate uncertainty (arcsec)
55769.579379	6.307842	29.413369	0.15
55771.604166	6.292654	29.425701	0.04
55771.605415	6.292632	29.425695	0.04
55771.606501	6.292635	29.425715	0.04
55771.607663	6.292621	29.425726	0.04
55771.608740	6.292620	29.425727	0.04
55771.609935	6.292599	29.425734	0.04
55771.611162	6.292590	29.425738	0.04
55777.429249	6.241761	29.457017	0.15
55777.432170	6.241731	29.457031	0.15
55779.429720	6.221865	29.466342	0.15
55779.432634	6.221833	29.466356	0.15
55805.378961	5.868124	29.517194	0.15
55805.381869	5.868073	29.517191	0.15
55805.529037	5.865584	29.517108	0.15
55805.531951	5.865535	29.517104	0.15
55823.328227	5.548573	29.474693	0.15
55823.331638	5.548508	29.474683	0.15
55823.385840	5.547476	29.474463	0.15
55823.388756	5.547422	29.474449	0.15
56163.513767	6.946110	30.082751	0.04
56165.452640	6.916665	30.084417	0.04
56165.453721	6.916659	30.084404	0.04
56165.454800	6.916640	30.084412	0.04
56165.455882	6.916628	30.084416	0.04
56165.456987	6.916619	30.084414	0.04
56165.458064	6.916592	30.084418	0.04
56165.459158	6.916565	30.084416	0.04
56165.460234	6.916565	30.084412	0.04
56165.461314	6.916549	30.084408	0.04
56165.469550	6.916410	30.084426	0.04
(225088) 2007 OR10			
55766.416929	334.910094	-13.958308	0.08
55766.422054	334.910058	-13.958326	0.08
55771.515914	334.864568	-13.974438	0.04
55771.516976	334.864570	-13.974449	0.04
55771.518146	334.864541	-13.974452	0.04
55771.519315	334.864544	-13.974448	0.04
55771.520406	334.864551	-13.974467	0.04
55771.521585	334.864509	-13.974438	0.04
55771.523067	334.864503	-13.974461	0.04
55771.524242	334.864509	-13.974482	0.04
55777.419374	334.809116	-13.993759	0.08
55777.423444	334.809076	-13.993773	0.08
55779.417995	334.789760	-14.000428	0.08
55779.422065	334.789714	-14.000439	0.08
55807.314056	334.504747	-14.094050	0.08
55807.318130	334.504705	-14.094063	0.08
55807.530686	334.502484	-14.094744	0.08
55807.534751	334.502441	-14.094755	0.08
56161.394827	334.840370	-13.786288	0.04
56161.395965	334.840359	-13.786293	0.04
56161.397133	334.840337	-13.786293	0.04
56161.398291	334.840337	-13.786296	0.04
56161.399438	334.840326	-13.786317	0.04
56162.468039	334.829289	-13.789909	0.04
56162.469176	334.829260	-13.789913	0.04

TABLE 2 (*Continued*)

MJD	α (deg) ^a	δ (deg) ^a	Coordinate uncertainty (arcsec)
56163.325587	334.820436	−13.792798	0.04
56163.326731	334.820429	−13.792796	0.04
56163.327896	334.820403	−13.792800	0.04
56165.369806	334.799285	−13.799639	0.04
56165.370963	334.799272	−13.799655	0.04
56165.372043	334.799253	−13.799670	0.04
56165.408962	334.798865	−13.799799	0.04
56165.410042	334.798870	−13.799776	0.04
56165.411124	334.798834	−13.799786	0.04
56165.412370	334.798838	−13.799788	0.04
56165.413446	334.798833	−13.799789	0.04
56165.414525	334.798829	−13.799789	0.04
56165.415866	334.798780	−13.799811	0.04
56165.416946	334.798782	−13.799783	0.04
56165.418031	334.798781	−13.799808	0.04
56165.419294	334.798737	−13.799794	0.04
56165.420371	334.798766	−13.799821	0.04
56165.421605	334.798737	−13.799824	0.04
56165.422682	334.798742	−13.799794	0.04
56165.423765	334.798713	−13.799820	0.04
56165.425020	334.798703	−13.799831	0.04
56165.426100	334.798679	−13.799841	0.04
56165.427368	334.798683	−13.799834	0.04
56165.428443	334.798684	−13.799849	0.04
56166.447938	334.788135	−13.803229	0.04
56166.449013	334.788127	−13.803240	0.04
56166.509245	334.787477	−13.803433	0.04
56166.549260	334.787059	−13.803579	0.04
56167.385009	334.778460	−13.806341	0.04
56167.386086	334.778441	−13.806314	0.04

^a J2000 coordinates.

2.1. Point-Source Catalog Production

Software from the MegaPipe data pipeline (Gwyn 2008) was used to produce the point-source catalog and to astrometrically calibrate each of the MegaPrime images. Starting with images already preprocessed by the Elixir pipeline (Magnier & Cuillandre 2004a), for each image we produced a source catalog with positions in pixel coordinates using SExtractor (Bertin & Arnouts 1996). SExtractor's parameters were set such that only fairly bright sources were detected; the detection criteria are set to flux levels 5 sigma above the sky noise in at least five contiguous pixels. The catalogs were further cleaned of cosmic rays and extended sources, leaving only point sources. Source centroids were found using SExtractor's simple centroid method. More complicated methods such as Gaussian or PSF fitting were found to provide no noticeable benefit.

Each of the pixel coordinate catalogs were matched to an external astrometric catalog, either the SDSS or 2MASS (Skrutskie et al. 2006). The SDSS DR9 (Ahn et al. 2012) provides a superior source density, and very small astrometric errors (0.07–0.09"). Where it was not available, 2MASS was chosen as the reference catalog (astrometric error 0.08–0.09").

We did not use UCAC (Zacharias et al. 2004) because it is fairly shallow; most of the sources are saturated in MegaPrime images, leaving too few sources for accurate astrometric calibration. The USNO catalogs were also considered: they go deeper and have a higher source density. The astrometric errors (0.4–0.6") on each source are larger than with the 2MASS catalog. Empirically, it was found that using the 2MASS catalog gave the smallest astrometric residuals.

Initially, the pixel coordinate catalogs were matched to the external astrometric catalog on a chip-by-chip basis. The initial Elixir (Magnier & Cuillandre 2004b) preprocessing done by CFHT provides an initial astrometric calibration, which is typically accurate to better than 1". The matching is therefore relatively simple. Sophisticated techniques (such as the quad-matching method used by Lang et al. 2010) are not required. During the initial matching process, any catalog source that was more than 1" away from the nearest observed source was ignored. Once the catalogs were matched, the transformation was computed. For the initial match, we used a second-order polynomial in x and y . This transformation was used to refine the matching of sources in the images to sources in the external catalog, and the transformation was recomputed. The second transformation was computed slightly differently. The MegaPrime distortion map can be adequately described by a polynomial with second and fourth order terms in measured radius, r , measured from the center of the mosaic. This is given by

$$R = r(1 + a_1 r^2 + a_2 r^4), \quad (1)$$

where R is the true radius, and a_1 and a_2 are distortion coefficients. The coefficients of this polynomial were determined for all 36 chips simultaneously. In addition, a linear distortion map was computed for each chip. The combination of a global, non-linear transformation and 36 local, linear transformations sufficiently describes the distortion, such that additional complexity in the map does not detectably improve the solution. The global transformation takes care of most of the distortion caused by the MegaPrime optics, while the linear transformation takes care of any non-coplanarity of the detector array as well as the effects of differential refraction. We avoid the usually adopted method of determining the full distortion map which uses a third-order polynomial transformation for each chip. This utilizes up to 20 parameters per chip, or a total of 720 parameters for all 36 chips. This number of parameters is uncomfortably close to the number of sources available for astrometric calibration. In most MegaPrime fields of view one typically finds 2000 suitable sources, but the number can be as low as 1000.

Once transformations had been determined, they were used to convert the pixel coordinates in the individual source catalogs to R.A. and decl. The catalogs from each image were merged to produce a master catalog. For each source from each catalog, all the catalogs are checked for matching sources. A match occurs if a source in one catalog lies within 2" of a source in another

catalog. The matching sources must also have measured magnitudes within 1 mag of each other. Once all the matching sources had been found, their measured positions from the different catalogs were averaged. To avoid confusion in the matching, if two sources in the same catalog lie within 4" of each other, both sources are discarded.

Next, the astrometric calibration of each input image was repeated using the merged master catalog as the astrometric reference. Using these new calibrations, the source catalogs for each image are converted from pixel coordinates to R.A. and decl. These catalogs are merged as described previously to produce a new merged master catalog. This second catalog is used to calibrate the images a third time. We refer to this step as "merge-by-catalog".

The images were photometrically calibrated by one of three methods:

1. If the images overlapped the SDSS, it was used for calibration. To account for slight differences in photometric systems due to detector and filter differences, the SDSS photometry was transformed to the MegaPrime system as follows:

$$r_{\text{Mega}} = r_{\text{SDSS}} - 0.024(g_{\text{SDSS}} - r_{\text{SDSS}}). \quad (2)$$

This results in an absolute photometric calibration accurate to about 0.01 mag.

2. If the image lay outside the SDSS, the Elixir photometric calibration was used for data taken on photometric nights. The absolute photometric calibration in this case is slightly worse, typically 0.03 mag.

3. Images taken on nonphotometric nights were calibrated using parts of the image which overlapped with images photometrically calibrated with one of the previous methods.

The photometrically calibrated catalogs were merged using a similar method to the astrometric catalog merging described above to produce a merged master photometric catalog. The final photometric calibration was done using this catalog. Merging the photometric catalogs and recalibrating in this way does not significantly improve the external photometric calibration, but ensures that the internal image-to-image zero-point calibration is typically better than 0.005 mag.

The astrometrically and photometrically calibrated images were then combined using SWarp (Bertin 2004). SWarp is a program that resamples and stacks multiple images onto a projection defined by the image world coordinate systems. The background was computed on a 128 pixel grid using a median filter and removed. The astrometric distortion was removed and the photometric scaling was applied. The images were resampled to a common grid using a Lanczos 3 pixel kernel. The scaled, resampled pixels are combined using a median. We refer to this step as "merge-by-pixel". SExtractor was then run on the resulting image to produce the final catalog of point sources which we refer to as the Master Point Source Catalog (MPSC).

Finally, the individual images were re-calibrated using the MPSC as an astrometric reference.

After each iteration of the astrometric calibrations, the image-to-image astrometric residuals were checked. After the initial match to the external catalog, the astrometric residuals range from 0.08 to 0.1" rms, typically slightly higher if the 2MASS catalog was used as an external reference, slightly lower if the SDSS was used. After using the second master catalog, the one generated using the "merge-by-catalog" method, the astrometric residuals are $\sim 0.06''$. The residuals get marginally lower if the merge-recalibrate-merge cycle is repeated. After using the final "merge-by-pixel" master catalog the astrometric residuals are typically 0.03–0.04" between two individual images. The residuals between the individual images and the corresponding master catalog are typically 60–70% smaller than residuals between two individual images.

Figure 2 shows the astrometric residuals between two input images after matching to the "merge-by-pixel" master catalog. The top left plot shows the astrometric residuals as a vector field. The lengths have been greatly exaggerated. The bottom left plot shows the residuals in R.A. and decl. as a scatter plot. Histograms of the residuals in both directions are also plotted.

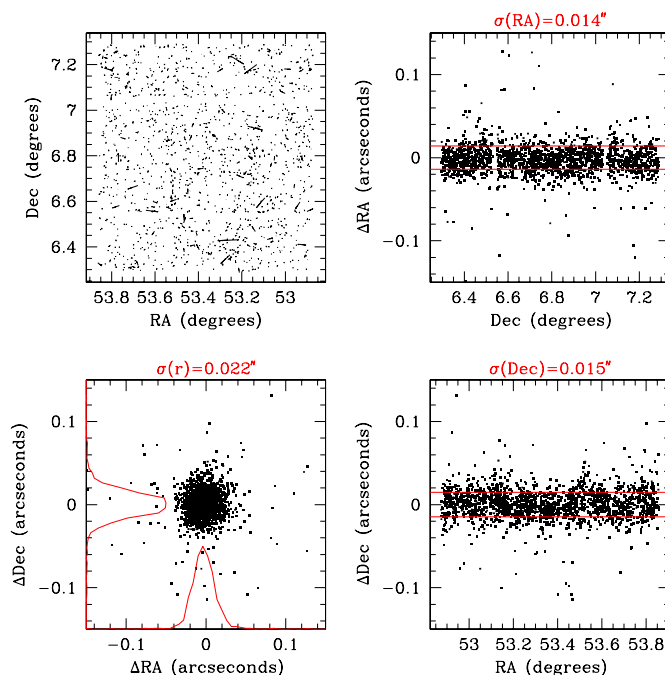


FIG. 2.—Astrometric residuals between two input images after matching to the "merge-by-pixel" master catalog. *Top left*: The astrometric residuals as a vector field. Lengths have been exaggerated for visual clarity. No patterns or trends in the residuals are apparent. *Bottom left*: Residuals in R.A. and decl. Histograms of the residuals in both directions are also plotted. The title shows the standard deviation of the combined R.A. and decl. squared sum of the residuals. *Right*: Residuals in R.A. as a function of decl. and residuals in decl. as a function of R.A. The horizontal lines mark plus or minus 1 standard deviation from the mean of the residuals, the values of which are shown in the titles. See the online edition of the *PASP* for a color version of this figure.

The two plots on the right show the residuals in R.A. as a function of decl. and the residuals in decl. as a function of R.A. The residuals are seen to be on the order of $0.02''$, while there are a few misidentifications (indicated by the outliers in the scatter plots and by longer than usual lines in the vector field), no large systematic shifts are apparent.

When the KBO of interest fell in one of the CFHT images, its position was measured with respect to the MPSC. For astrometry of the KBOs measured in the CFHT data, we adopt an uncertainty of $0.04''$, typical of the astrometric residuals found after the “merge-by-pixel” step, the last step in producing the MPSC.

2.2. Gemini Observations

Along with the target astrometry provided by the MegaPrime data, additional astrometry of the targets was measured from images taken with the GMOS detector (Gemini program GN-2011B-Q-60). Each target was visited multiple times. During each visit, a pair of images was taken with small $\sim 30''$ dither between pairs. All exposures were taken in r' -filter and exposure times were tuned such that the resultant photometric signal-to-noise ratio (S/N) was ~ 40 – 50 . This ensured that the resultant astrometric error was dominated by the match between the images and the MPSC and not by the quality of the object measurement. The target’s observed positions are presented in Table 2.

After standard image reductions (bias removal and flat fielding) the astrometric plate solutions for the GMOS data were found by matching those images to the MPSC. The match was done with the use of SCAMP (Bertin 2006). SCAMP is a program that produces astrometric solutions which match one point source catalog to a reference catalog. During the matching process, each image was treated individually, providing as independent individual astrometric measurements as possible. The plate solution of GMOS was found to be adequately described by a simple CD matrix solution; utilizing higher-order terms revealed no improvement in the astrometric solution. Experience has shown that SCAMP typically produces unreliable astrometric uncertainties. That is, the root mean square (rms) astrometric scatter of a solution is typically erroneous in one of two ways. Either the reported rms is small despite the fact that the astrometric solution is clearly erroneous, or the rms value is found to be significantly smaller than the scatter in repeat images of the same targets. Repeated measurements of a KBO at a given epoch have demonstrated that the plate solutions provided by SCAMP result in a $\sim 0.08''$ scatter in the astrometry of the tracked KBOs. Therefore, we forgo use of the quoted SCAMP RMS values, and adopt an astrometric uncertainty of $0.08''$ for all GMOS measurements.

2.3. Orbital Element Correction

The second step in occultation predictions is the generation of accurate ephemerides. As discussed in § 1, a common

approach is what we refer to as the constant offset method, in which the nominal ephemerides of the targets in question are offset by a value representative of the typical differences between the observed and predicted positions of the object.

One merit of the constant offset method comes as a result of the use of a nominal ephemeris for the target object. By use of a previously determined ephemeris, all past reported astrometry and an orbit determination from those data are automatically considered in the predictions. While it is certainly true that past astrometry are typically not of the quality required for occultation predictions, many measurements spanning a multiyear baseline provide modestly accurate ephemerides that, with small astrometric corrections, can be suitable for occultation predictions.

The accuracy of predictions made by the constant offset method primarily suffer from one major issue. In reality the difference between the nominal-offset ephemeris and the true ephemeris is not actually constant. The difference between the two ephemerides depends primarily on the quality of the nominal ephemeris. A small error in the nominal ephemeris can result in both a periodic shift (with period of a year) and a nearly linear shift between the nominal-offset ephemeris, and the true ephemeris (see Fig. 1). Even for the best ephemerides, the amplitude of the periodic offset can be of order $\sim 0.02''$. As a result, without frequent tracking and updates to the offset, predictions with this method can be unreliable.

A different technique involves adjustment of the orbital elements of the nominal ephemeris to match available astrometry. That is, with appropriate tweaks to the nominal orbital elements, the ephemeris itself can be corrected and used directly for occultation predictions. We consider the orbital element adjustment approach and its comparison with the constant offset method here.

We start with the orbital elements provided by the astDys catalog and make use of Orbfitter¹⁶ in calculating ephemerides. To determine the appropriate orbital element corrections, we adopt a maximum-likelihood approach. Specifically, given adjustments to the semimajor axis, eccentricity, inclination, longitude of ascending node, argument of perihelion, and mean anomaly $\delta a, \delta e, \delta I, \delta \Omega, \delta \omega, \delta M$, we adopt the log-likelihood

$$L(\delta a, \delta e, \delta I, \delta \Omega, \delta \omega, \delta M) = P(\delta a, \delta e, \delta I, \delta \Omega, \delta \omega, \delta M) - \frac{1}{2} \sum_i \left(\frac{\cos \beta_i (\alpha_i - \bar{\alpha}_i)}{\sigma_{i,\alpha}} \right)^2 + \left(\frac{\beta_i - \bar{\beta}_i}{\sigma_{i,\beta}} \right)^2, \quad (3)$$

where α_i and β_i are the i th observed R.A. and decl. of the object, and $\bar{\alpha}_i$ and $\bar{\beta}_i$ are the R.A. and decl. predicted from the

¹⁶ See <http://adams.dm.unipi.it/orbfit/>.

adjusted ephemeris of the object in question. The terms $\sigma_{i,\alpha}$ and $\sigma_{i,\beta}$ are the astrometric uncertainty of the i th measurement (recall that we adopt 0.04" and 0.08" uncertainty in the MegaPrime and GMOS observations, respectively).

In equation (3), $P(\delta a, \delta e, \delta I, \delta \Omega, \delta \omega, \delta M)$ is the log-prior on the orbital elements. For this, we turn to the element errors in the nominal ephemeris. We however, choose not to apply any priors on the orbital element angles. This decision is motivated by the consideration of the coordinate origin of the astrometric catalog (2MASS or SDSS), which we first consider when generating the MPSC. Each catalog will have a slightly different coordinate origin. The ephemerides provided by astDys reference a different zero point (usually that defined by the USNO A catalog). As a result of the differing origins, the orbital angles Ω , ω , and M , are incorrect at the level of accuracy required. Similarly, as the nodal angle has changed, so has the orbital inclination. It is only the semimajor axis and eccentricity that are not affected by adjustment of the reference. We adopt Gaussian priors on a and e with standard deviations equal to the uncertainties in those elements provided with the astDys ephemerides.

When determining the orbital element corrections with equation (3), we only consider the MegaPrime and GMOS observations we gathered ourselves and matched to the MPSC. These observations only span 1–2 years, and as a result partially avoid potential zonal errors which affect the astDys orbital elements. The disadvantage of this approach is that past observations are not directly used by our method. Rather, those data are only used as a prior, a choice which reflects how much prior information we can safely extract from the nominal astDys elements without producing unreliable results.

To converge on a maximum likelihood, we utilize MCMC Hammer (EMCEE, Foreman-Mackey et al. 2012). MC Hammer is an affine invariant Markov Chain Monte-Carlo sampler that rapidly converges on the maximum likelihood solution in a minimum number of steps. For the routine, we adopt 100 walkers, and utilize a 100 step burn-in phase. During the maximization, EMCEE determines the autocorrelation time, τ —the number of steps required such that further samples are independent and distributed as the posterior likelihood function. Thus, the routine must be run for multiple τ to ensure that the likelihood space is accurately evaluated. For all orbital elements, τ was found to be ~ 5 –8. Thus, our routine was run for 150 steps after the burn-in phase, or roughly 20 or more autocorrelation times. Additional steps were found to not improve the resultant likelihood evaluations.

As an endproduct of this routine, we can extract confidence intervals on each of the orbital elements. From these confidence intervals, we can determine the astrometric uncertainty on the target for any future date and time. No direct method of positional astrometric uncertainty can be generated from the constant offset method.

To compare the performance of the constant offset and element adjustment methods, we set up a theoretical situation. For

this example, we consider a theoretical Eris, and assigned as its elements the elements reported by astDys for the real Eris. Using Orfit, we then simulated the historical observations of the theoretical KBO on the dates of all reported astrometry for the real Eris—the dates were extracted from the Minor Planet Center.¹⁷ We note that Orfit includes planetary perturbations, a necessary consideration for the decades-long arcs of the KBOs we consider. Noise was added to the simulated observations to account for typical random uncertainties in reported astrometry. A Gaussian distribution with standard deviation 0.3" in both R.A. and decl. was used. We also attempted to include zonal errors in the simulated observations. This was done by scattering the observations by a small value every time the theoretical KBO moved more than 3°; we adopted a Gaussian distribution with width 0.08" in both R.A. and decl. In a similar vein, we generated fake tracking observations (like those we present from MegaPrime and GMOS) adopting 0.04" astrometric uncertainties.

For the theoretical KBO, a set of orbital parameters was determined from the simulated historical observations with Orfit (ignoring the simulated tracking observations), the same routine used for the astDys elements. We then utilized our maximum likelihood approach to determine $(\delta a, \delta e, \delta I, \delta \Omega, \delta \omega, \delta M)$, the six element corrections which provided the best match to the simulated tracking observations. We also evaluated the best offset which minimized the residuals between the simulated tracking observations and the nominal ephemeris.

The results of our simulation are shown in Figure 1, where we compare the results of both ephemeris correction processes. This figure clearly demonstrates one of the difficulties with occultation predictions. Both methods suffer from a 365 day period oscillation in the difference between the predicted and actual ephemerides. In addition, the constant offset method suffers from an increasing error in decl. with time.

One advantage of the element correction approach is clear. The approach can produce more accurate ephemerides further away from the last epoch of observation than the constant offset method. The quality of our element correction approach however, depends critically on the quality of the astDys ephemeris. In addition, without sufficient baseline in the astrometry used in equation (3), the resultant element offsets can be incorrect; simulations suggest that at the very least, 1 year baselines are required. The element correction approach is also sensitive to discrepant tracking astrometry which can result in ephemerides that quickly deviate away from the true ephemeris. Because the constant offset method averages all tracking astrometry, this method is much less sensitive to discrepancies in the tracking observations.

Which of the constant offset method or the element adjustment approach produces the most reliable occultation predictions

¹⁷ See <http://www.minorplanetcenter.org/iau/mpc.html>.

will be different for each object, and the determination of which essentially requires future observations. Eventually, the element adjustment approach should surpass the constant offset method. How long is required is not easily determined a priori, but simulations suggest a ~ 2 year baseline or longer will allow the element adjustment approach to surpass the constant offset method. Both methods however, suffer from different effects, and as a result, comparison of occultations predictions produced with both methods should be considered until the results of the element adjustment approach have been demonstrated to be superior on an object by object basis. Thus, we choose to present the results of both methods when reporting candidate occultations.

It should be noted that, along with the ephemeris uncertainty, there is also uncertainty in the stellar astrometry. From the data used in generating the MPSC, each star is observed multiple times, with a positional accuracy of $\sim 0.04''$ in both R.A. and decl. The quoted stellar position represents a global mean of each measurement. As we will discuss further below, it appears that the uncertainty on the mean position does not decrease as the square-root of the number of times the star is observed, but rather, appears roughly a factor of 2 worse than that expectation.

2.4. Proper Motions and Chromatic Differential Refraction

During the generation of the MPSC, we make no effort to account for the effects of proper motion, or chromatic differential refraction. The first effect, that of proper motions, was ignored during our analysis because proper motions were not determined for either of the reference catalogs we used. As a result, the stars used in the first step of the astrometric calibration will have moved slightly since they were observed by 2MASS (1997–2001) or the SDSS (2000 to present). Estimates of the proper motion of sources in the 2MASS catalog are available from the PPMXL catalog (Roesser et al. 2010). Experimentation with that catalog revealed that the proper motions measured by PPMXL were only accurate enough to improve the positions of the brightest sources in the 2MASS catalog, those which were primarily saturated in our observations. No noticeable improvement in positional accuracy of fainter sources from which our astrometric solutions were derived, was found. As a result, we chose to adopt the cataloged positions for the first stage of our astrometric calibrations and make no effort to correct for proper motions.

Tholen et al. (2013) point out that not considering proper motions can result in zonal errors. In the small fields we observe to produce the MPSC, these zonal errors would manifest themselves as a nearly constant systematic offset between the frame of the reference catalog (2MASS or SDSS) and the frame of the MPSC. The offset will be nearly constant across the small fields covered by the MPSC for each object.

To determine if ignoring proper motions could result in inaccurate predictions, we performed a test of the predictions for the object 2002 TC302, in which the positions of stars in the

reference catalog (2MASS) were scattered to mimic the effects of proper motions. The distribution of proper motions was extracted from the PPMXL catalog in a 2° -wide patch around the position of the KBO. The R.A. and decl. positions of each source were then randomly scattered according to the distribution of R.A. and decl. proper motions. Analysis of the PPMXL proper motions suggest that $\sim 15\%$ of sources have moved more than $1''$ since the 2MASS catalog was created, and hence would be ignored during the MPSC generation. After the sources were randomly scattered, this number increased by a factor of $\sim \sqrt{2}$. The full occultation predictions routine (MPSC generation, determination of KBO astrometry, and ephemeris correction) was then applied using the randomized reference catalog. As predicted, compared to the astrometry referenced to the non-scattered 2MASS catalog, a systematic offset in both the MPSC source positions and that of the KBO were found, with amplitude of nearly $0.1''$ R.A., and $0.05''$ decl. In addition, the astrometry from the scattered catalog had a slope of $\sim 0.05''$ per degree of R.A. in both the R.A. and decl. axes. The effects of the offset and slope produced a shift of ~ 300 km in the predicted shadow tracks of 2002 TC302. Even the most accurate predictions have ~ 1000 km uncertainties in the shadow path, which is entirely a result of ephemeris uncertainty. As ephemeris uncertainty grows rapidly with time away from the last tracking observation, the prediction errors induced by not accounting for proper motions will always be small compared to the ephemeris error.

The reason why not accounting for proper motions has such little effect on the predictions can be easily understood. Recall that during the MPSC generation, an external catalog is only used in the first stage of generating astrometric solutions. An internal catalog is used in later stages to refine those solutions and generate a self-consistent MPSC. As a result of this internal reference to the observed sources, small variations in the solution caused by proper motions are reduced at each subsequent iteration of our calibration routine, mitigating these issues. In general, as shown by our test with 2002 TC302, this systematic offset does not significantly affect the quality of the astrometric solution or the KBO ephemeris as the astrometry of both the MPSC and the KBO are equally affected by the offsets.

While proper motions in general do not affect the quality of the astrometric solution, they will cause a degradation of some individual predictions with time away from the observations used to generate the MPSC. Take for example, a star with proper motion of $0.1'' \text{ year}^{-1}$ —roughly 15% of all stars have at least this proper motion. At the time of observation of that star for MPSC generation, its position is known to the precision of the MPSC. At typical KBO distances, the high proper motion of the star will have moved the shadow track more than 1000 km from that predicted in just 6 months. Clearly, advanced monitoring of the target stars is warranted for particularly profitable events.

Like proper motions, we make no effort to account for the effects of chromatic differential refraction (CDR), primarily due

TABLE 3
 REFINED ORBITAL ELEMENTS

Object	a (AU)	e	i (deg)	Ω (deg)	ω (deg)	M (deg)	
(50000) Quaoar	43.1881^{+7}_{-22} 0.0002	0.037213^{+6}_{-13} 0.000004	7.9948^{+1}_{-1} 0.0002	189.004^{+3}_{-4} 0.004	162.72^{+6}_{-2} -0.01	276.06^{+2}_{-6} 0.01	2MASS
(84522) 2002 TC302	55.763^{+7}_{-11} 0.022	0.2968^{+7}_{-1} -0.0008	34.98787^{+61}_{-7} 0.00058	23.8299^{+2}_{-1} 0.0007	85.69^{+14}_{-3} -0.22	320.439^{+2}_{-46} 0.081	2MASS
(90377) Sedna	543.4^{+16}_{-2} -0.3	0.85965^{+46}_{-8} -0.00007	11.928240^{+5}_{-18} 0.000057	144.428^{+1}_{-3} 0.007	310.944^{+34}_{-8} -0.004	358.215^{+7}_{-1} -0.001	SDSS
(136199) Eris	68.011^{+2}_{-3} 0.000	0.43578^{+3}_{-2} -0.00000	43.8451^{+8}_{-16} 0.0007	36.0509^{+8}_{-4} -0.0004	150.80^{+1}_{-1} -0.00	202.76^{+3}_{-4} 0.01	SDSS
(136472) Makemake	45.488^{+1}_{-1} -0.003	0.16143^{+1}_{-2} 0.00001	29.01313^{+1}_{-8} 0.00012	79.2848^{+12}_{-2} -0.0020	296.80^{+2}_{-3} -0.03	154.22^{+4}_{-3} 0.05	SDSS
(202421) 2005 UQ513	43.512^{+1}_{-1} -0.005	0.14391^{+8}_{-6} 0.00001	25.72627^{+4}_{-14} -0.00022	307.8351^{+3}_{-9} -0.0012	220.02^{+4}_{-6} 0.04	221.72^{+8}_{-6} -0.05	SDSS
(225088) 2007 OR10	66.96^{+1}_{-1} 0.00	0.50195^{+9}_{-14} 0.00000	30.8137^{+8}_{-8} 0.0025	336.8390^{+1}_{-1} -0.0006	206.78^{+1}_{-2} 0.01	102.61^{+6}_{-4} -0.02	2MASS

NOTE.—Epoch of coordinates 56200.0 MJD. Offsets are with respect to the astDys nominal orbits on 2012 September 1. Displayed uncertainties are in the last decimal place. Where necessary, multiple significant digits were included to reflect asymmetric uncertainties. Second row for each target displays the adjustment from the initial astDys elements.

to the single band observations we acquired for MPSC generation. Our observations were taken over a broad range of airmasses, but less than 2 in all cases. In the standard conditions on Mauna Kea (Cohen & Cromer 1988), the reddest stars, with $(V - I) \sim 3$, will experience a shift of amplitude $\sim 0.05''$ at an airmass of 2 compared to its relative position when observed at zenith (Stone 1984; Monet et al. 1992). For most stars, $(V - I) \approx 0.8$ resulting in a shift is of order $0.01''$. The reddest KBOs eg. Quaoar and Sedna with $(V - I) \sim 1.3$, will experience a slightly larger shift. The primary consequence of CDR is a fundamental limit on the precision of the MPSC; unless observations of the MPSC sources are taken at random airmasses, their astrometry cannot be more precise than the shift cause by CDR at their average observed airmass. For most stars, and our observations, we conservatively estimate the amplitude of this effect at up to a $\sim 0.02''$ shift of individual stars compared to the astrometry of the KBO. Improvements beyond this limit cannot be made, unless either the effects of CDR are accounted for, requiring multiband observations, or observations that are restricted to a small range in airmasses.

3. THE PREDICTIONS

Both the constant offset method and our element correction routine were used to produce occultation predictions for the seven targets of this study. The resultant best-fit orbital elements—taken as the MCMC point with highest likelihood—are presented in Table 3.¹⁸ A few notable predictions are presented

in Table 4. The residuals of the element correction approach are presented in Figures 3–9.

It is important to note that the coverage of the future tracks by our MPSC is different for each object. For instance, for Eris, the occultations can be predicted as far into the future as 2015 January 1. For Sedna, however, this is only 2014 June 1. Efforts will be made to ensure future coverage will be made available. As a practical limit, we only report candidate occultations by stars with magnitude brighter than $r' = 21$.

An example of a candidate occultation by 2007 OR10 is shown in Figure 10. The candidate star has $r' = 19.5$; and with predicted time roughly 2013 August 8 6:20 UT. The uncertainties presented in the prediction depend on the method. The uncertainties quoted by the element correction routine are the $1\text{-}\sigma$ scatter in R.A. and decl. produced by the MCMC fit, and for the constant offset method are just the rms residuals left in the astrometry of 2007 OR10. This candidate demonstrates an extreme case for the difference in predictions possible between the two methods, roughly 4000 km. The element adjustment approach suggests that the large discrepancy is caused by the oscillations between the true and predicted positions inherent to the constant offset method; a large offset of $\sim 0.05''$ occurs on this date. Only with observations near this event will this be confirmed.

4. CONFIRMATION

An occultation by the KBO Sedna was predicted to be visible over North America at 2012 Dec 26 03:40 UT of a star with $r' = 18.9$. Attempts to observe this event were made at various telescopes, including: the Plaskett telescope at the Dominion Astrophysical Observatory in Victoria, BC (WCF); the

¹⁸ All available occultations are presented at www.fraserkbos.com.

TABLE 4
NOTABLE PREDICTIONS

Star				Magnitude (r')	Shadow velocity (km s^{-1})	Vertical shadow uncertainty (km)
Object	Date (UT)	R.A. ^a	Decl. ^a			
2005 UQ513	2013/09/15 20:10	00 30 11.9	30 37 23.8	14.0	23.6	1000
2005 UQ513	2014/11/19 02:53	00 29 40.5	30 41 23.3	15.9	21.9	2500
Quaoar	2013/07/01 21:42	17 35 13	−15 23 33.9	17.5	24.5	1900
Quaoar	2013/07/09 02:41	17 34 40.5	−15 23 37.5	14.4	23.3	1800
Quaoar	2013/07/12 20:54	17 34 24.2	−15 23 43.2	12.9	22.8	1900
Quaoar	2014/09/10 02:35	17 37 32.3	−15 31 08.9	18.0	4.2	3200
Makemake	2014/03/20 20:28	12 48 28.3	26 40 36.1	19.8	26.3	1430
OR10	2013/08/04 06:19	22 20 57.9	−13 27 18.4	19.5	26.1	4300

^aJ2000 coordinates. Units of R.A. are in hours, minutes, and seconds, and units of decl. are degrees, arcminutes, and arcseconds.

University of Wyoming Infrared Telescope, near Laramie, WY (LAY); The R.A. Cross Telescope near Calgary, BC (PPL); the Las Cumbres Observatory Global Telescope at McDonald Observatory (TL and FBB); the Astrophysical Research Consortium Telescope at Apache Point (RJM); the Vatican Advanced Technology Telescope at Mount Graham (RPB); and the Perkins Telescope at Lowell Observatory (MJB). Unfortunately, a widespread storm system prevented useful data from being collected from any site.

Some confirmation of the accuracy of the predictions has been made possible from the observation of three candidate occultations of the object Quaoar made by the Gemini telescopes.

Two candidates were observed on 2012 July 6 and July 13 by the Gemini-South telescope of stars with $r' = 20.0$ and 20.2 , respectively (Gemini program GS-2012A-DD-4). The third candidate was of a $r' = 16.37$ magnitude star observed by the Gemini-North telescope on 2012 July 10 (Gemini program GN-2012A-DD-5). Observations were made with the GMOS cameras roughly 1–2 hr before and after the nominal event times; pairs of images with 40 s exposure times in the r' filter were taken. These allowed us to accurately measure the occultation impact parameter of each event. The events themselves were observed with the acquisition cameras in the R-filter in windows approximately 20 minutes in length centred on the nominal event times. These observations will be reported in

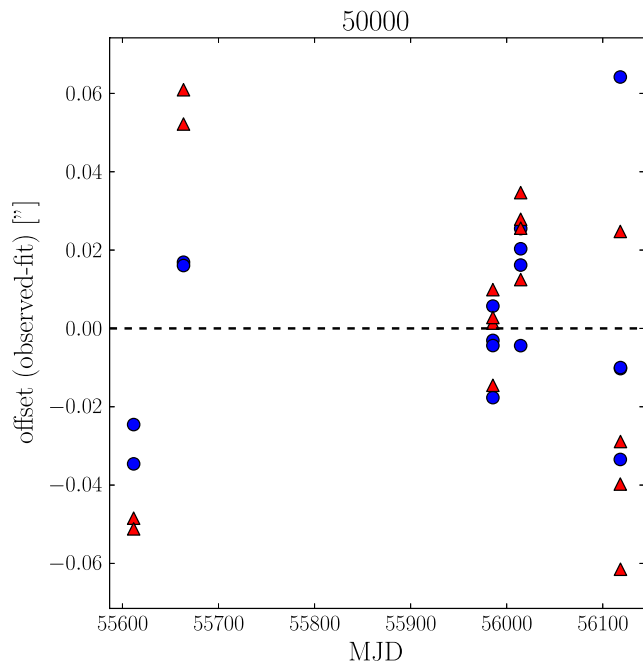


FIG. 3.—Astrometric residuals in arcseconds as a function of date of observation after application of the element correction approach for (50000) Quaoar. Residuals in R.A. and decl. are shown as blue circles and red triangles, respectively. See the online edition of the *PASP* for a color version of this figure.

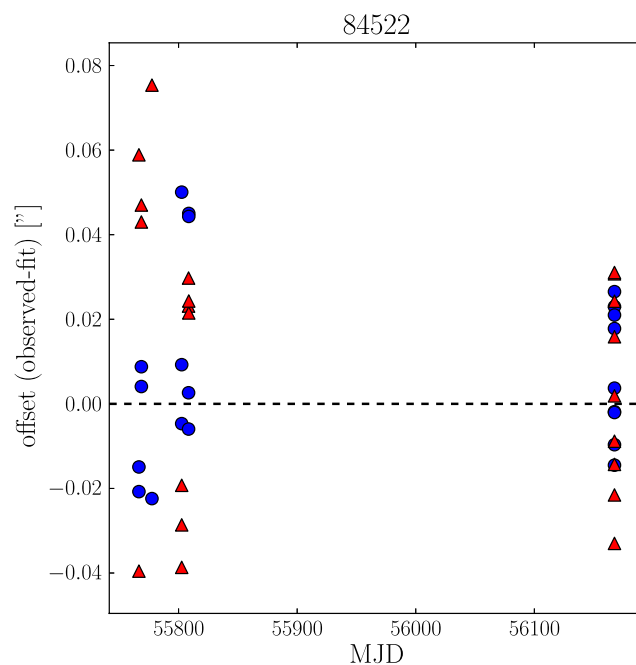


FIG. 4.—As in Figure 3 but for object (84522) 2002 TC302. See the online edition of the *PASP* for a color version of this figure.

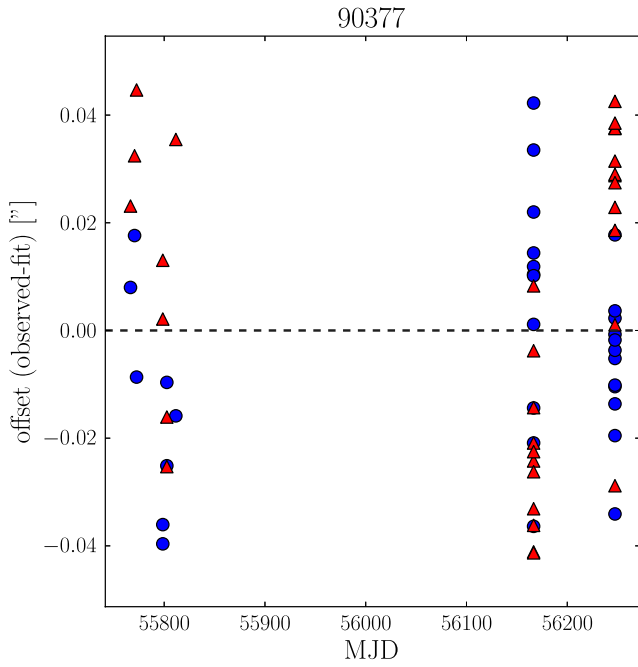


FIG. 5.—As in Figure 3 but for object (90377) Sedna. See the online edition of the *PASP* for a color version of this figure.

a separate manuscript. Weather frustrated the observations on July 6; no useful data was acquired on that date.

Predicted offsets between Quaoar and the target star at the time of GMOS observations for the July 10 and 13 events

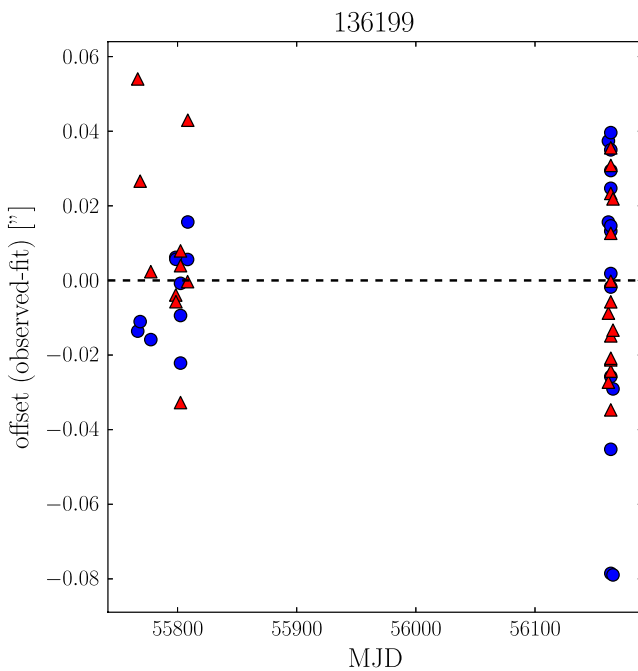


FIG. 6.—As in Figure 3 but for object (136199) Eris. See the online edition of the *PASP* for a color version of this figure.

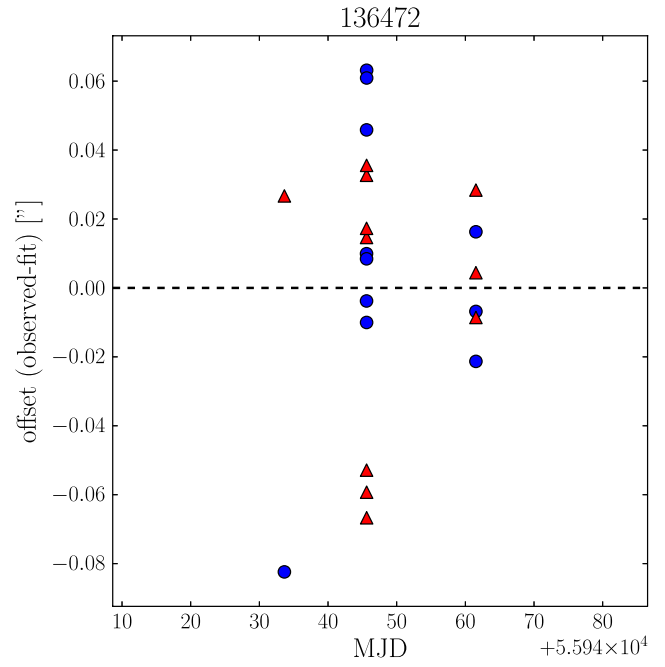


FIG. 7.—As in Figure 3 but for object (136472) Makemake. See the online edition of the *PASP* for a color version of this figure.

are presented in Table 5. Observed offsets were measured using the IRAF *daophot* Gaussian centroid routine (Tody 1993). The observed offset between Quaoar and the target star in each image are reported in Table 5. Using these measured offsets,

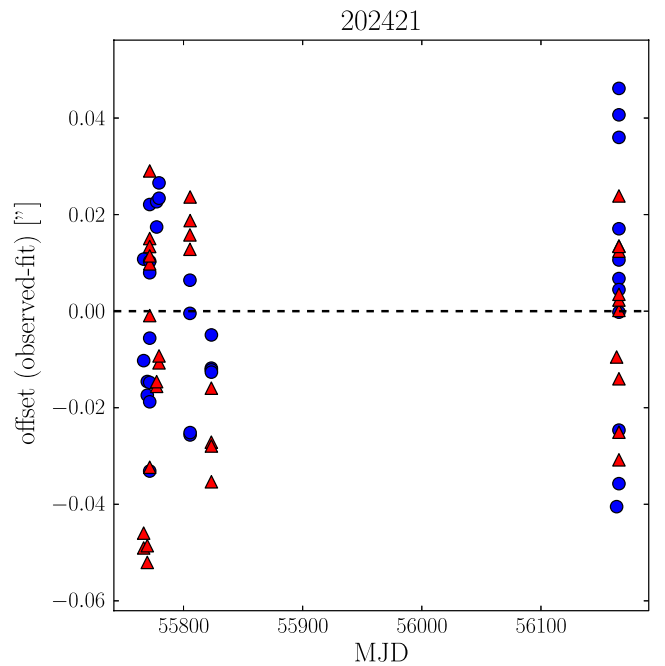


FIG. 8.—As in Figure 3 but for object (202421) 2005 UQ513. See the online edition of the *PASP* for a color version of this figure.

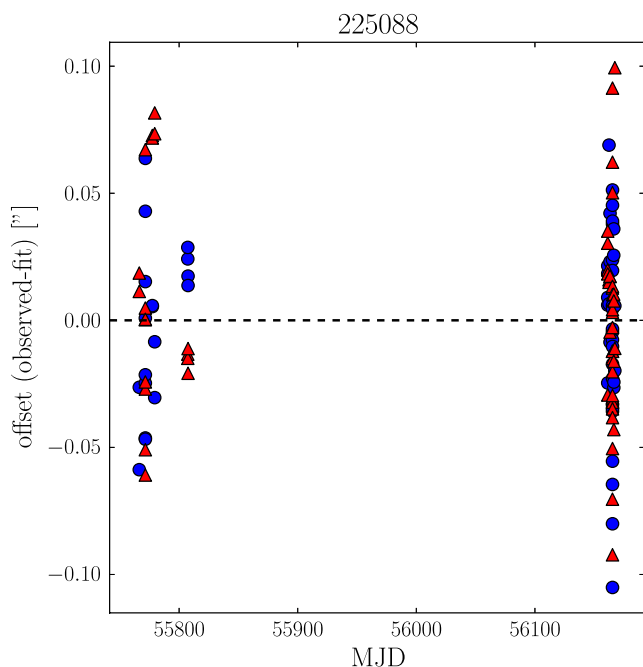


FIG. 9.—As in Figure 3 but for object (225088) 2007 OR10. See the online edition of the *PASP* for a color version of this figure.

Quaoar's impact parameter for each event was determined by fitting a straight line to the observed offsets and finding the closest point between the line and star position. Uncertainties on the impact parameters were then found by a Monte Carlo approach. For each of the four offset measurements, a random point was generated within the measurement uncertainties, and the impact parameter of that random realization was found. This process was repeated to 1000 times to generate a range of impact parameters consistent with the observations. We quote the

TABLE 5
OBSERVED AND PREDICTED OFFSETS FOR (50000) QUAOAR

Time (UT)	R.A. (arcsec)		Decl. (arcsec)	
	Observed	Predicted	Observed	Predicted
2012 July 10				
6.856185	4.04 ± 0.1	4.03	-0.00 ± 0.1	0.067
6.895627	3.97 ± 0.2	3.94	-0.00 ± 0.2	0.066
11.145036	-7.43 ± 0.1	-7.63	-0.21 ± 0.1	-0.12
11.178836	-7.54 ± 0.08	-7.72	-0.20 ± 0.08	-0.12
2012 July 13				
2.707929	4.49 ± 0.06	4.45	0.14 ± 0.06	0.14
2.759136	4.36 ± 0.08	4.31	0.13 ± 0.08	0.13
6.324234	-4.88 ± 0.2	-5.07	-0.12 ± 0.2	-0.09
6.375295	-5.02 ± 0.15	-5.20	-0.11 ± 0.15	-0.10

NOTE.—Offsets are determined from the element adjustment approach and are quoted as Quaoar-star. For R.A. units are seconds and for decl. units are arcseconds.

standard deviation of these realizations as the uncertainty on the event impact parameters. Diagrams presenting Quaoar's trajectory with respect to the target stars are shown in Figure 11.

The July 13 event was predicted to have an impact parameter of $0.017 \pm 0.03''$ and $0.0''$ from the element adjustment and constant offset methods respectively. The observed impact parameter was $0.019 \pm 0.004''$, in excellent agreement with the element adjustment approach.

The July 10 event was predicted to have an impact parameter of $0.012 \pm 0.03''$ and $0.03''$ from the element adjustment and constant offset methods respectively. The measured impact parameter was $0.076 \pm 0.005''$. This result may be interpreted that for this event, the constant offset method produced a more accurate prediction. Given the short 3 day interval between the events on July 10 and 13, the difference between the true

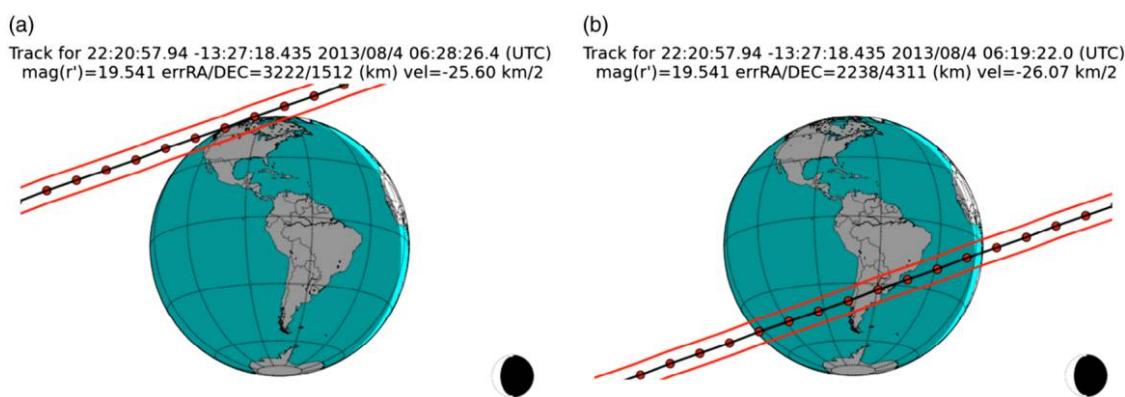


FIG. 10.—Example prediction for occultation by object 2007 OR10. Predictions using the element correction approach and constant offset method are shown in (a) and (b), respectively. Properties of the event, including star position and brightness, nominal occultation center time and velocity, and an estimate of the uncertainty are presented. Nominal shadow extent shown with red lines. Red dots are spaced 1 minute apart. Day–night terminator and moon phase are shown at the nominal occultation center time. Positional uncertainty of each method is shown. OR10 is assumed to be 1200 km in diameter. See the online edition of the *PASP* for a color version of this figure.

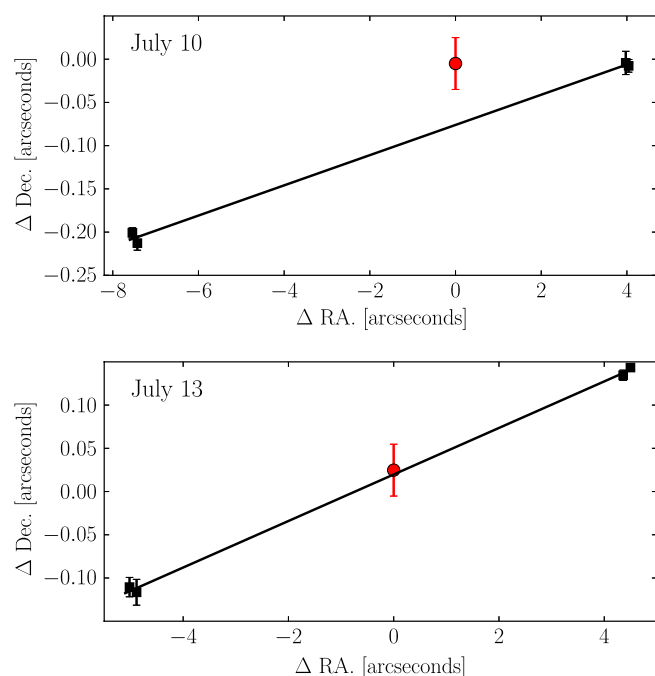


FIG. 11.—Diagrams showing distance of closest approach for the July 10 (*top*) and July 13 (*bottom*) events. Measured offsets (Quaoar-Star) are shown as *black squares*. Quaoar's inferred trajectory is shown as the *black line*. The closest approach predicted by the element adjustment approach is shown as the *red circle*. The uncertainty on the predicted impact parameter only includes that derived from the element correction approach, and does not include the uncertainty in target star position. *Note:* uncertainties in R.A. are smaller than the data points in this figure, but are the same size as the decl. uncertainties. See the online edition of the *PASP* for a color version of this figure.

ephemeris and those produced by the constant offset method are virtually the same on both days. As a result, each method must produce predictions of similar quality on July 10 as they produced for July 13. It must be that the position of the July 10 target star was not sufficiently well known.

The July 10 target star has been tentatively identified with a star in the USNO catalog with colour $(R - I) \approx 0.4$. Comparison with Quaoar, $(R - I) = 1.3$, suggests that CDR may result in a shift of as much as $\sim 0.015''$; CDR cannot account for the observed discrepancy in the target star's position with respect to Quaoar. It may be that the star had a high proper motion. To account for the discrepancy, the star would need to have a proper motion at least $0.2'' \text{ year}^{-1}$. The fraction of stars with proper motion at least that high is only 10%. Thus, it seems unlikely that proper motions are the cause of the discrepancy. Recall that the adopted uncertainty in position from the MPSC is $0.04''$. Scaling this value by 6, the square root of the number of MegaPrime observations of the star, the expected astrometric uncertainty on the star is $\sim 0.016''$. If this were the true stellar position uncertainty, then the observed impact parameter represents a more than $2-\sigma$ deviation from the prediction; it must be that the stellar astrometric uncertainty does not decrease as rapidly as \sqrt{N} . This suggests that in the MPSC generation, each

individual measurement of a star is not fully independent, but rather the measurements of a star are partially correlated. The true stellar astrometric uncertainty seems as much as a factor of ~ 2 larger than that expectation.

That the observed impact parameter of the July 13 event was in agreement with predictions demonstrates the utility of the element adjustment method in accurately predicting occultations. The observations reinforce the findings of our simulations. The element adjustment approach can be used to accurately predict stellar occultations. Until this approach has been shown to be superior for a particular object, other methods should also be considered alongside the element adjustment approach to gauge the uncertainty in a particular event. Further, our findings demonstrate the importance of knowing the stellar position, which can be as large as the uncertainty in the ephemerides. Our findings suggest that ~ 30 individual observations of a star will be required before its position is known to better than $0.01''$. This suggests that stellar position uncertainty can be the dominant factor in overall prediction uncertainty.

5. CONCLUSIONS

We have developed a new method of occultation predictions by which the cataloged orbital elements of Kuiper Belt objects are corrected for the difference between the ephemerides predicted by those elements, and the observed ephemerides. Observations of the fields occupied by seven well-tracked KBOs were acquired. From those observations, extremely accurate master point source catalogs were generated. We applied the element correction method as well as the standard constant offset method to the observations of the KBOs, and generated occultation predictions from both methods. The results of both methods were compared and it was found that the constant offset method suffers primarily from inaccurate cataloged ephemerides. We found that the element correction method suffers more from inaccuracies in the observations used to correct the orbital elements. For well tracked objects however, the element correction method seems to produce corrected ephemerides that degrade much more slowly with time than does the constant offset approach.

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